



# *A Modeling Framework for Coupled Natural-Human Systems*

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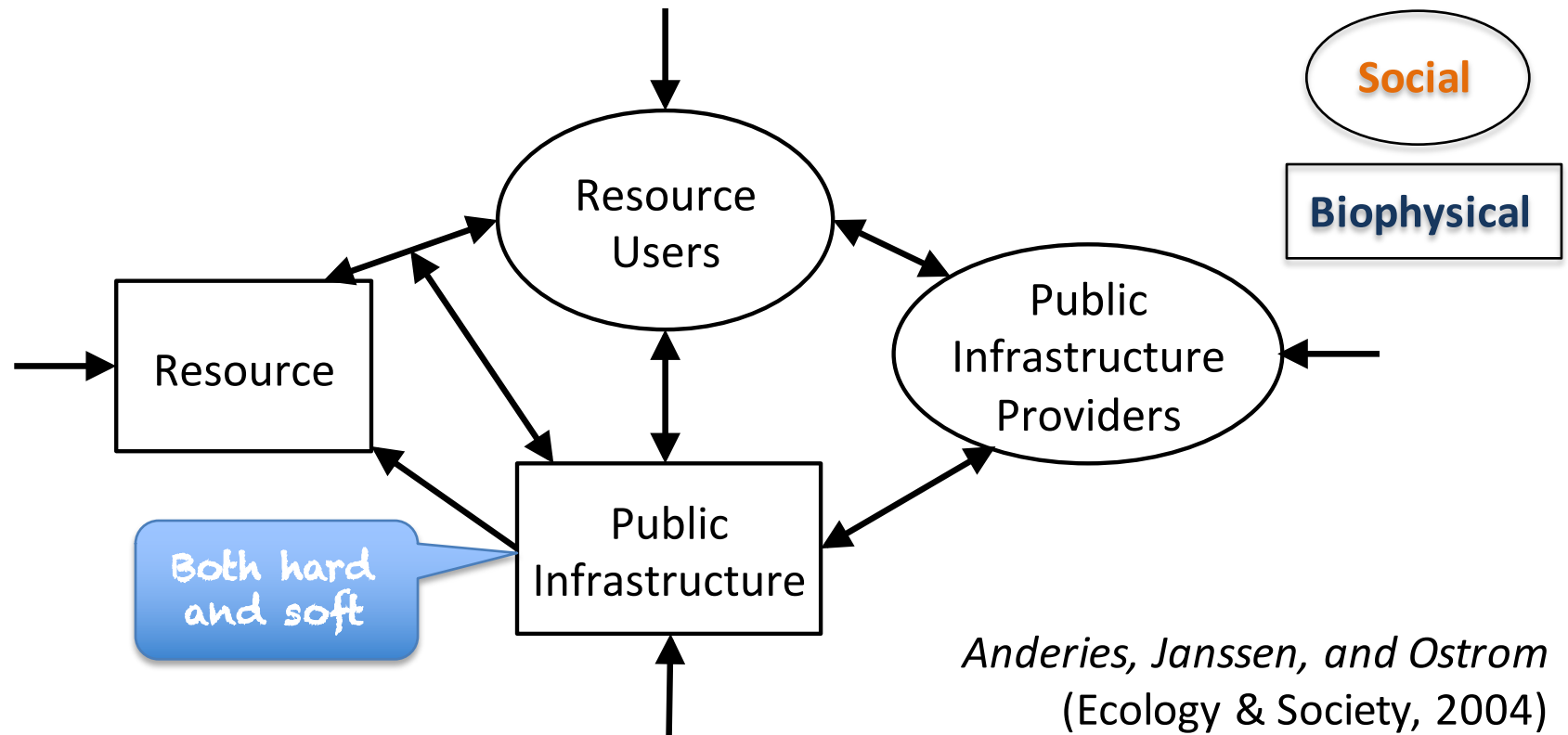
In collaboration with J. Marty Anderies

(School of Sustainability, Arizona State University)

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**NSF EPSCoR, Norman, OK**

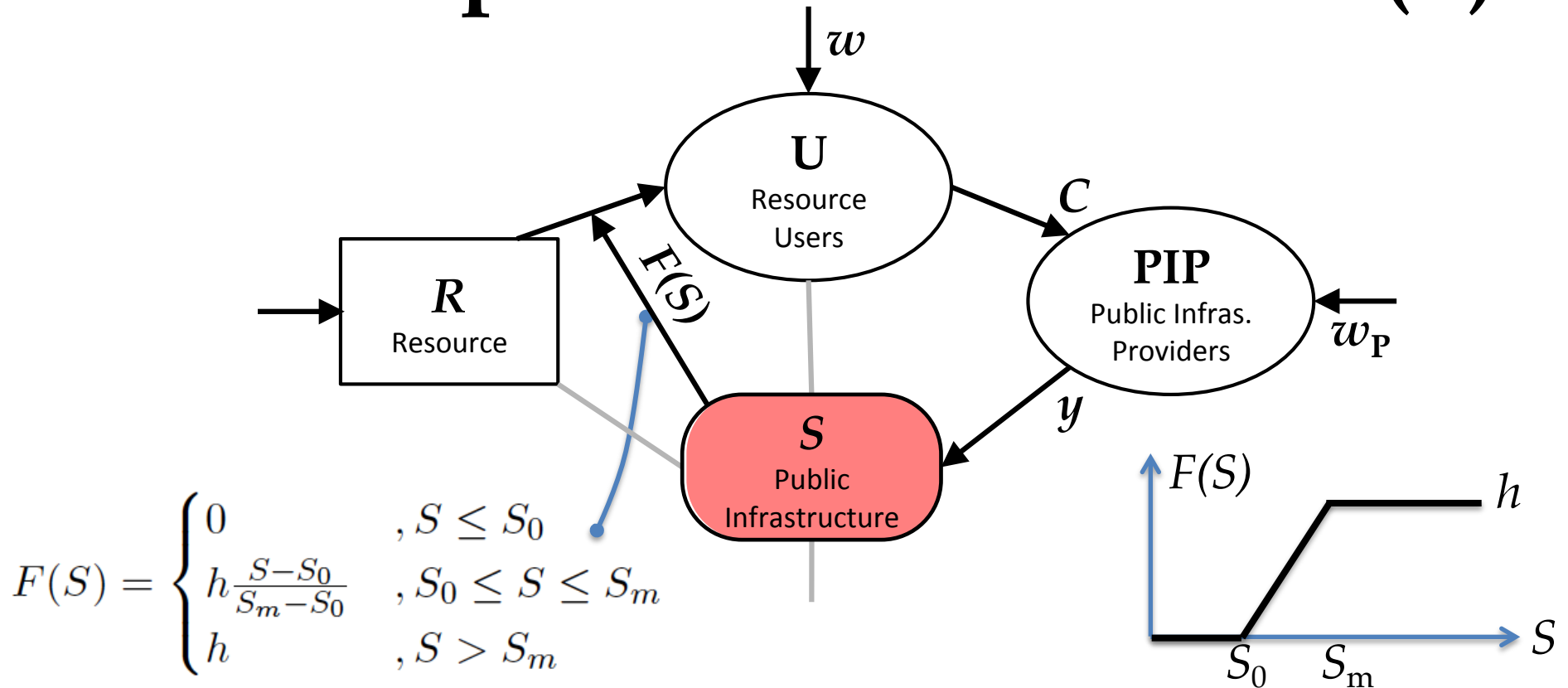
# Conceptual framework



**Goal:** Develop a unified theory of coupled natural-human systems

**Approach:** Systematically and mathematically operationalize the above conceptual framework

# State of public infrastructure (S)

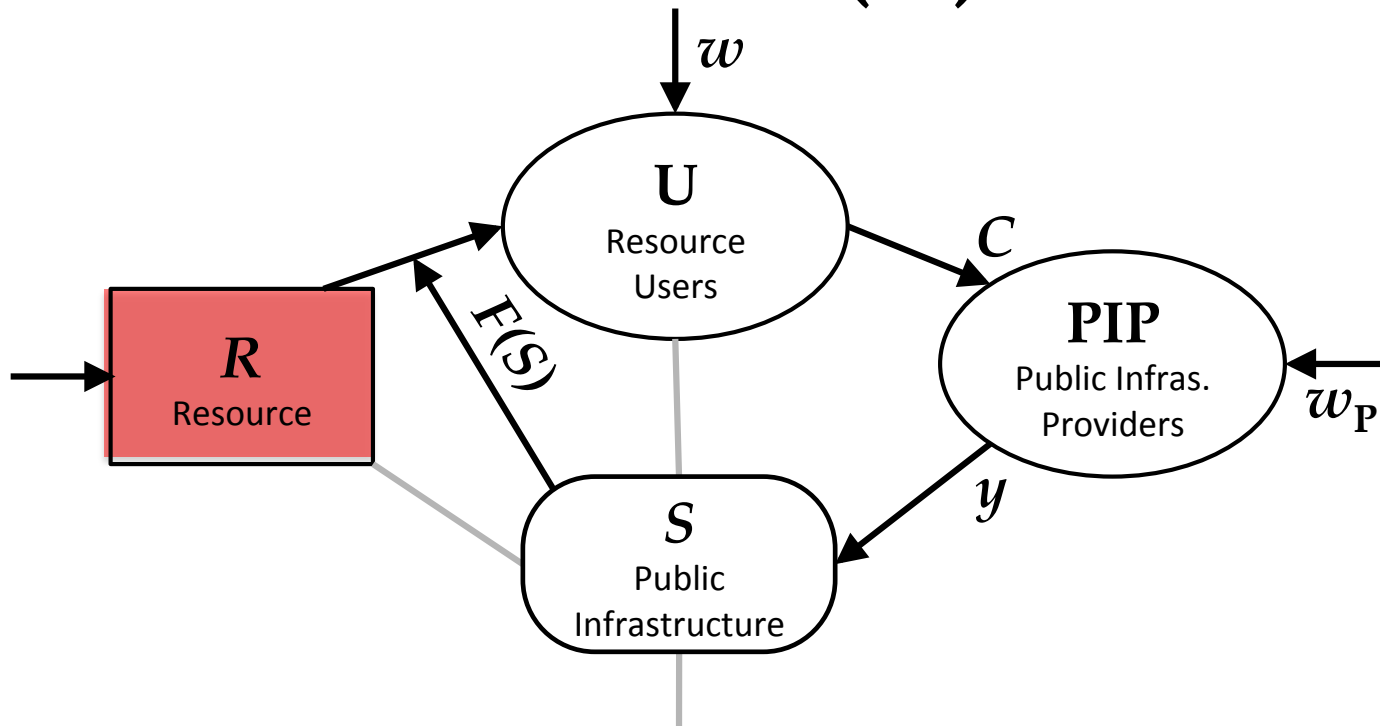


- ✓ Threshold behavior in its capacity—requires collective action
- ✓ Constant depreciation/decay—eventually collapses without maintenance

Maintenance    Decay

$$\frac{dS}{dt} = M(\dots) - \delta S,$$

# Resource (R)



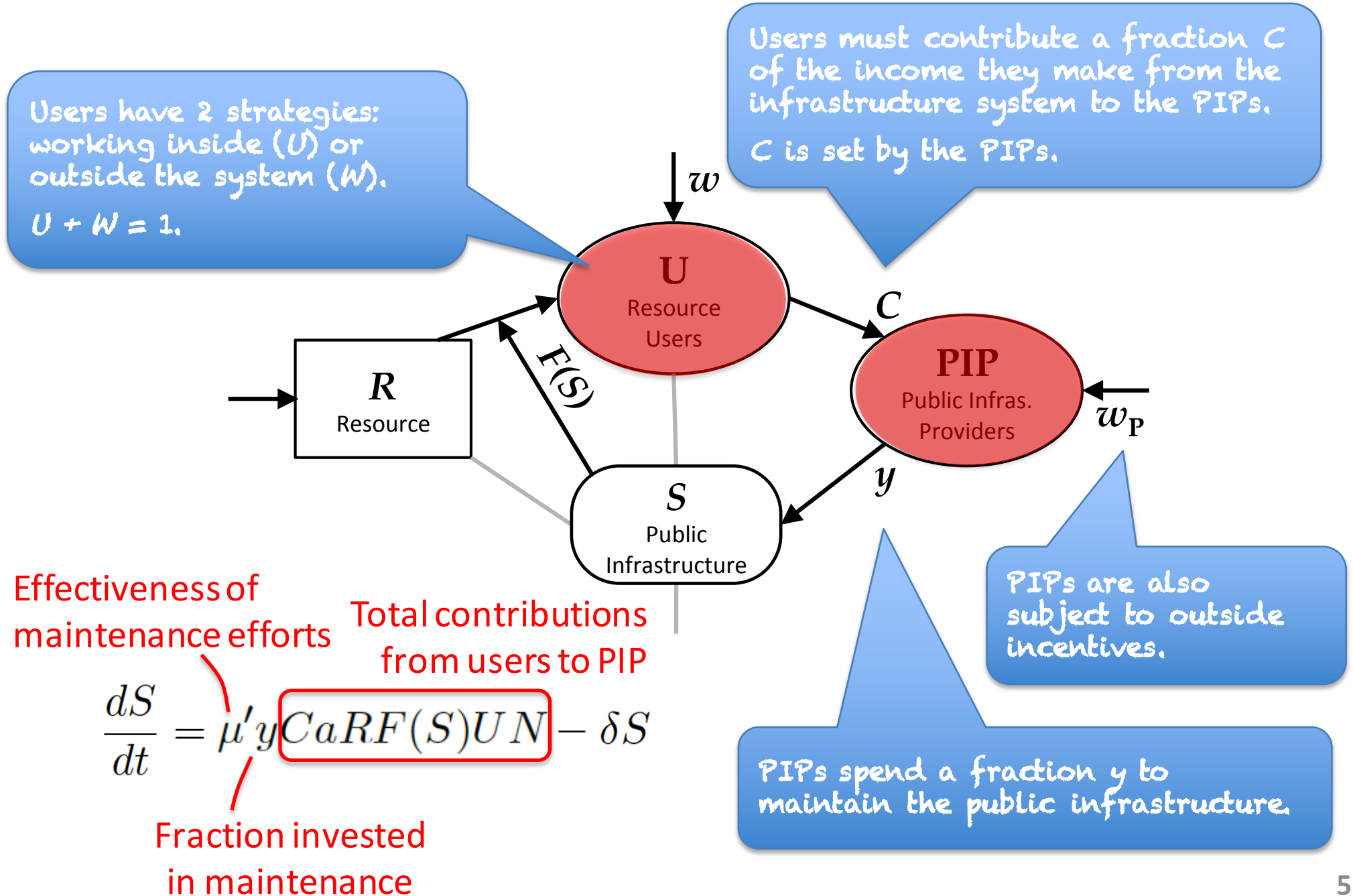
$$\frac{dR}{dt} = I - lR - \overset{\text{Usage rate}}{UN}F(S)R$$

Natural inflow

Natural loss (e.g.,  
ET, seepage)

Extraction by humans  
through infrastructure

# Two types of social actors: U and PIP



# Part self-organized, part designed

the challenge, regardless of the choice of analytical technology remains: How do we construct a version of (12–15) with the *right* level of complexity that is useful for development of policy that respects the fact that SES are partially self-organizing and partially designed. (SES = social-ecological systems)

(Anderies, Bull Math Biol 2015)

Replication (social learning)	Optimization
Boundedly rational	Rational
Myopic	Long-term
Self-organization	Design/planning

# Self-organizing Users *vs.* Optimizing PIP

Users self-organize through social learning (replicator dynamics):

$$\pi_U = (1 - C)aRh$$

$$\frac{dU}{dt} = rU(1 - U)(\pi_U - w)$$

*U increases when working inside pays better than working outside.*

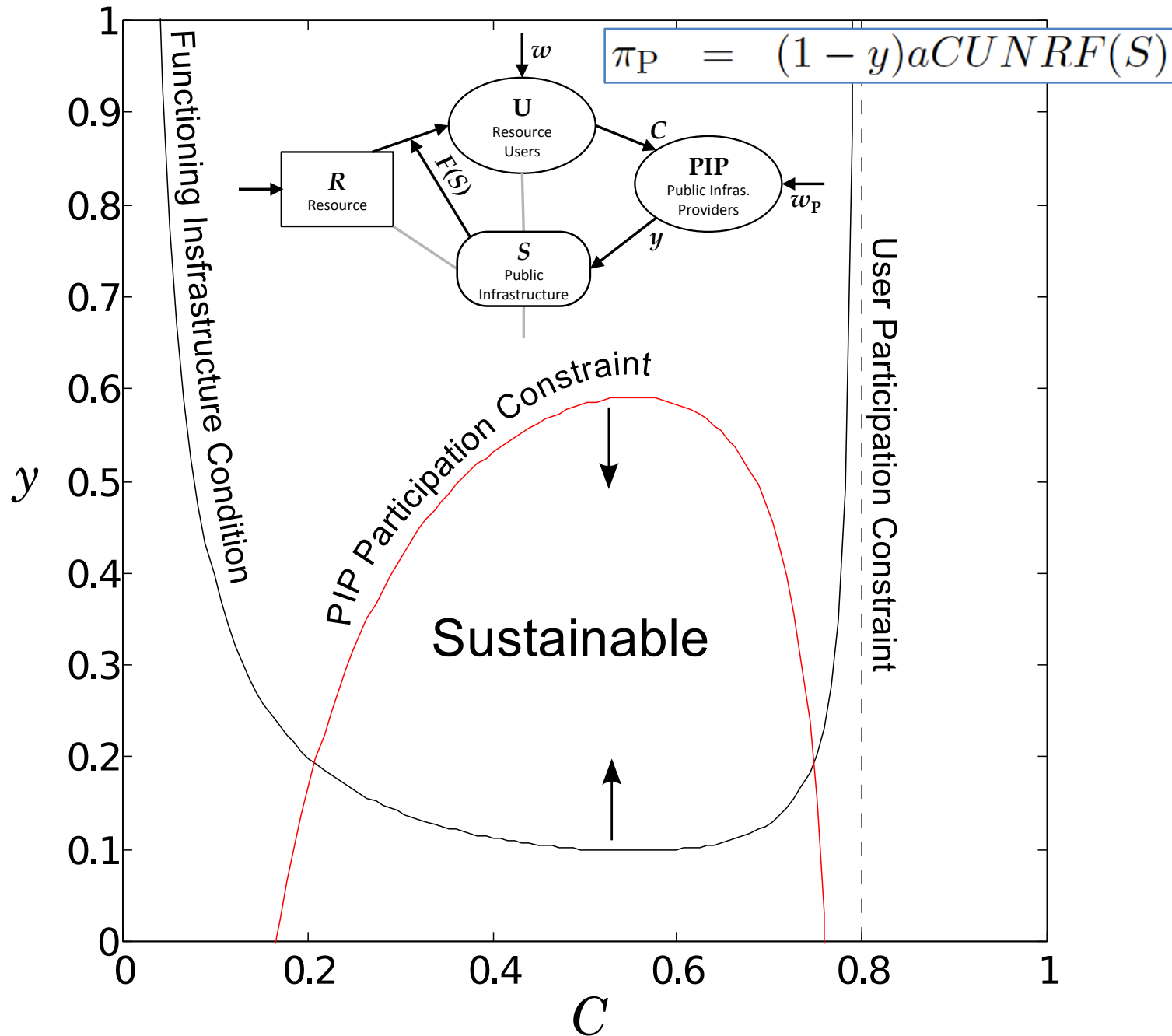
*It would increase fast if there are already a lot of existing adopters ( $U$ ) and potential replicators ( $1-U$ ).*

PIP optimizes its payoff:

$$\pi_P = (1 - y)aCUNRF(S)$$

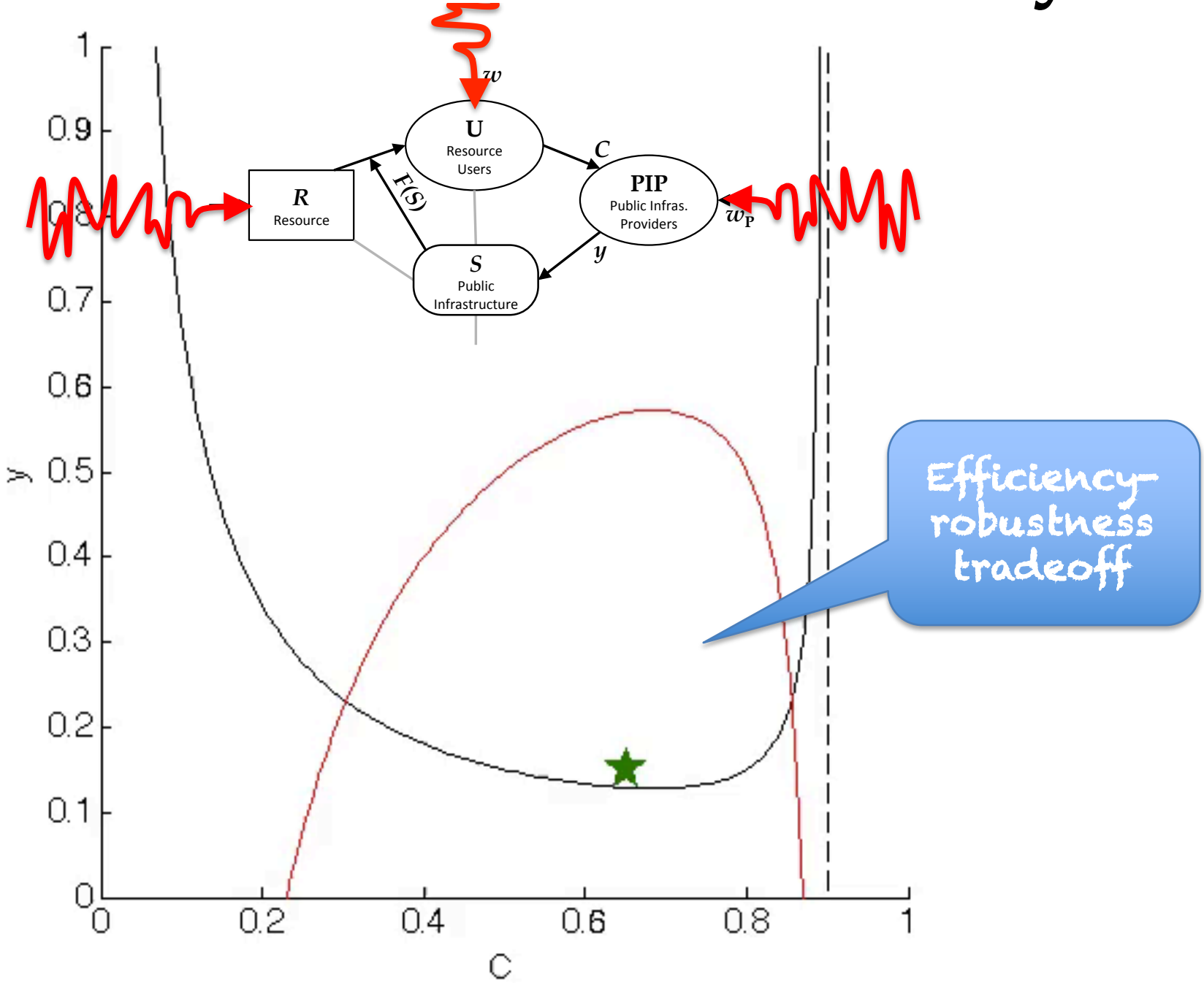
*PIP attempts to maximize their payoff by selecting  $C$  and  $y$ . But the users self-organize to respond to those "policies," which in turn affect the infrastructure functionality and resource availability.*

# PIP's $C$ - $y$ decision space

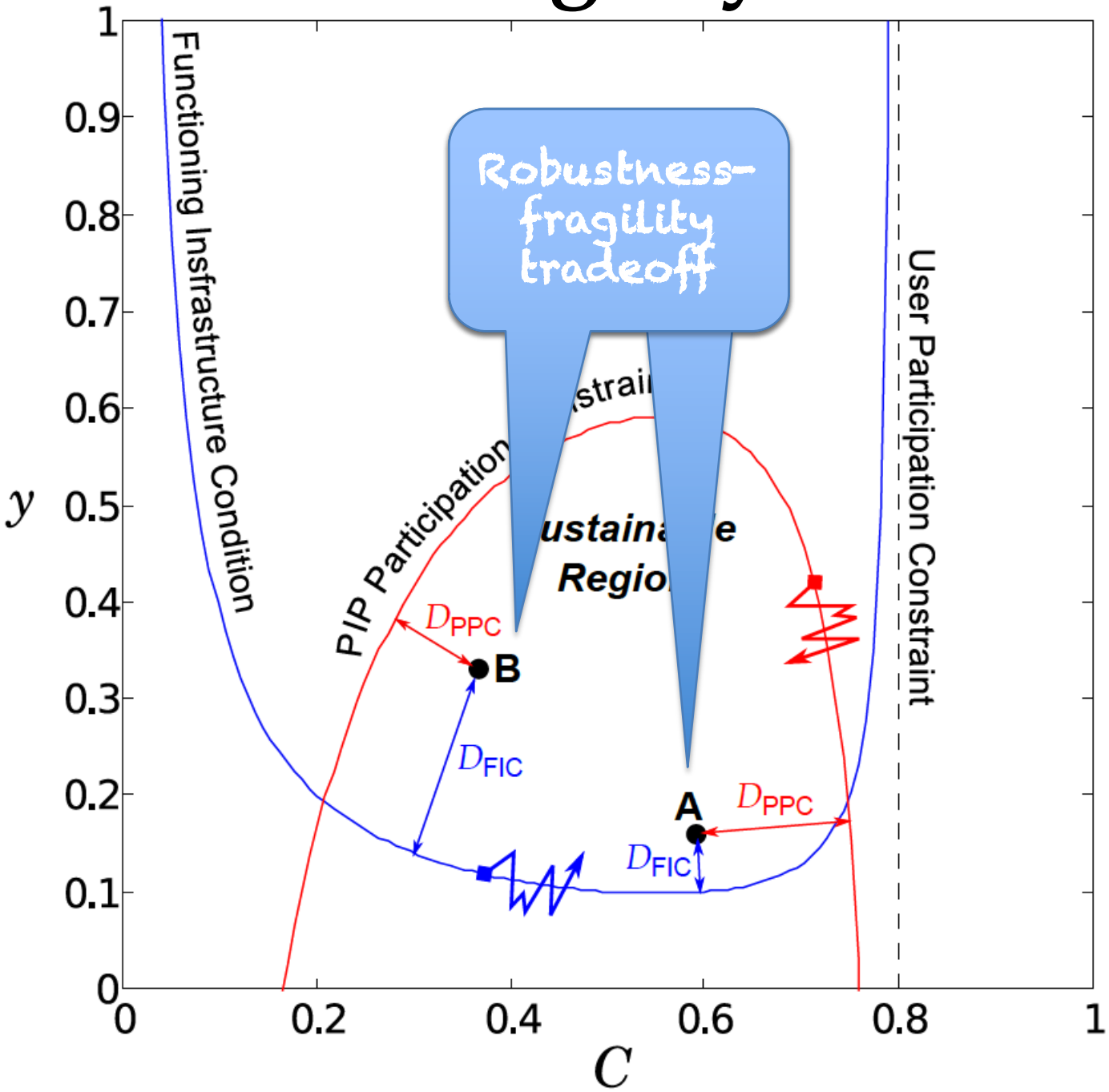




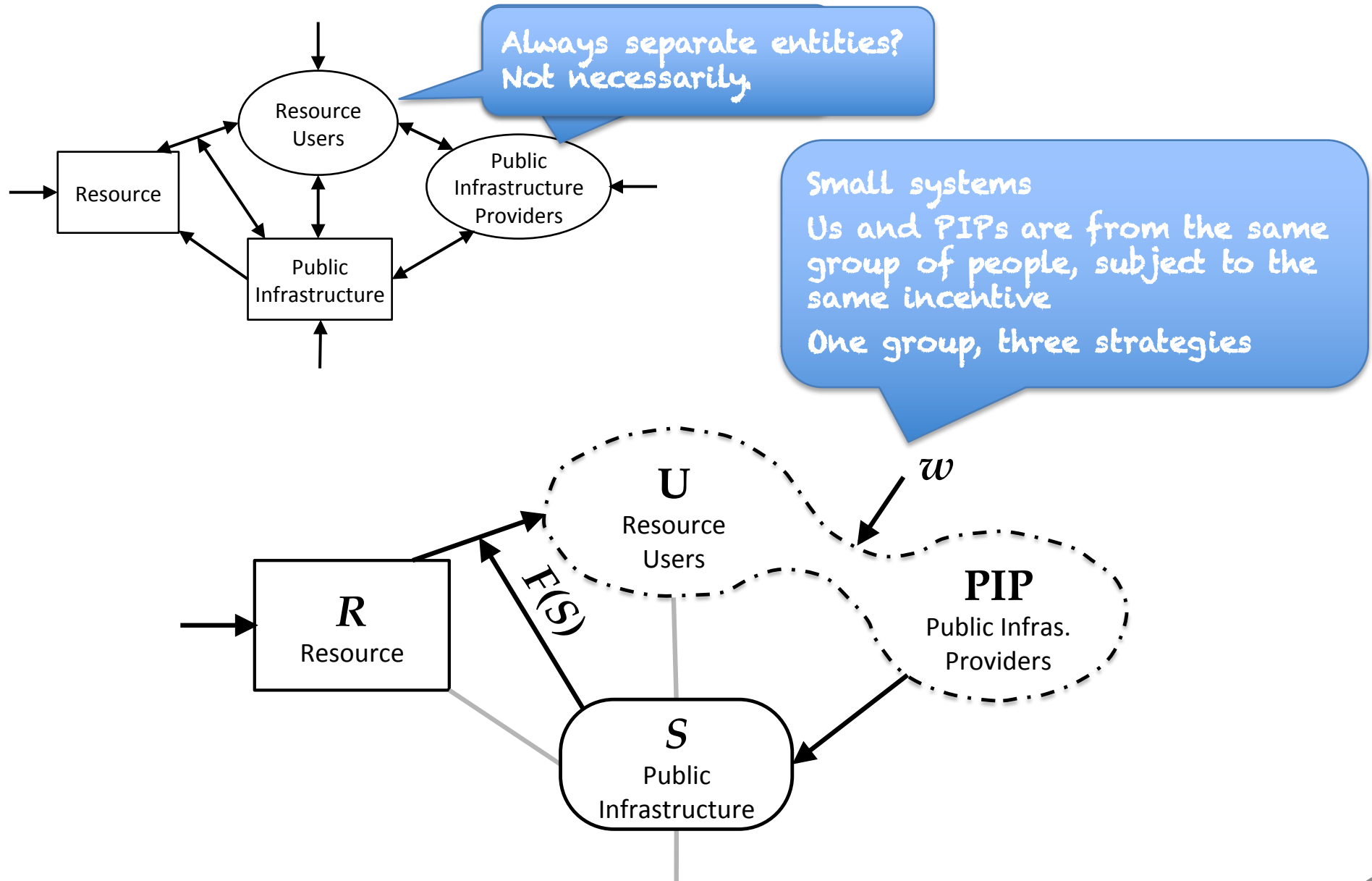
# Possible extension: variability



# Robustness-fragility tradeoffs



# Different social structure



# Summary



Resource, humans, & infrastructure, systematically combined;  
Interplays & dilemmas, mathematically defined.  
These systems are both designed and self-organized;  
With optimization & replication, they could be characterized.  
In a clear, simple model, constraints are made unambiguous;  
Important lessons are then brought to focus.  
Too much emphasis on performance and certain robustness,  
The system might be fragile against other stresses.  
With some key dynamics on a sound mathematical ground,  
Interesting questions and extensions abound.  
User diversity, resource variability, and other complexity...  
There is a lot of work we can expect to see.

Thank you for your attention.